

5633 Analysis of Algorithms – Spring 04

4/28/04

Material covered in class from 2/23/04 until 4/21/04

| Week | Material |
|-------|---|
| 7 | <p>Amortized analysis (Ch. 17.1, 17.2, 17.4; dynamic table slides) Aggregate analysis (total runtime of n operations), accounting method (prepay for later operations); binary counter, dynamic tables</p> <p>Red-black trees (Ch. 13.1, 13.2, 13.3) red-black tree property, rotations, insertion; abstract data types, ADT dictionary</p> |
| 8 | <p>B-trees (Ch. 18.1, 18.2) k-ary search trees, B-tree def., height, insertion</p> |
| 9 | <p>Dynamic programming (Ch. 15.2, 15.3, 15.4; slides) Fibonacci, binomial coefficient, LCS: fill table, then construct solution from the table; matrix chain multiplication; general outline of dynamic programming: Optimal substructure (recurrence), overlapping subproblems, fill table bottom-up or by memoization.</p> |
| 10 | <p>Computational Geometry (Ch. 33.2; slides) Range trees, preprocessing time, query time, space, line sweep, line-segment intersection</p> |
| 11/12 | <p>Minimum Spanning Trees (Ch. 23; slides) Prim, Kruskal</p> <p>Union-Find (Ch. 21.1, 21.2, 21.3; slides) Operations, list implementation, tree implementation, union-by-weight / union-by-rank, path compression. Ackermann function, and inverse Ackermann function α.</p> |
| 13 | <p>Single-source shortest paths (Ch. 24 without 24.4; slides) Optimal substructure, triangle inequality, relaxation step, Dijkstra (only for non-negative edge weights), predecessor tree (shortest path tree); Bellman-Ford, detection of negative-weight cycles; Shortest paths in a DAG</p> <p>All-Pairs Shortest Paths (Ch. 25; slides) Dynamic programming: Floyd-Warshall</p> |
| 14 | <p>P and NP (Ch. 34; slides) Decision problems, definition of classes P and NP, polynomial-time reductions; NP-hardness, NP-completeness; Show that problems are NP-complete by reducing from other problems; TSP, Clique, Independent Set, Vertex Cover, Hamilton Path, Hamilton Circuit</p> |

Relevant material for the final: Everything that we covered from the first day in class until (and including) NP-completeness. This means, everything that was relevant for the midterm **plus** everything on this page.

The final will be on **Tuesday May 4** from 8:30pm until 10:45pm in the classroom.