4/7/09



# 1. Adjacency matrix (3 points)

Give the adjacency matrix representation for the graph above. Assume that vertices are ordered alphabetically.

#### 2. Adjacency lists (3 points)

Give the adjacency lists representation for the graph above. Assume that vertices (e.g., in an adjacency list) are ordered alphabetically.

#### 3. Depth-first search (6 points)

Consider a depth-first traversal of the graph above, starting at vertex a. Assume the graph is given in your adjacency lists representation of question 2. Mark the results of the following subquestions in a copy of the drawn graph.

- (a) (2 points) Give the discover time (*d*-value) and the finish time (*f*-value) of each vertex.
- (b) (2 points) Draw the depth-first tree.
- (c) (2 points) Mark each edge with its DFS classification (tree edge, back edge, forward edge, cross edge)

#### 4. Breadth-first search (4 points)

Consider a breadth-first traversal of the graph above, starting at vertex *a*. Assume the graph is given in your adjacency lists representation of question 2. Mark the results of the following subquestions in a copy of the drawn graph.

- (a) (2 points) Give the visit time stamp for each vertex (according to the pseudo code on slide 7).
- (b) (2 points) Draw the breadth-first tree.

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# 5. Adjacency matrix (4 points)

Both breadth-first search (BFS) and depth-first search (DFS) assume that the graph is given in adjacency lists representation. Now, assume that the graph is given in an adjacency matrix.

- (a) (2 points) What part would change in the code for BFS? What would be the runtime for BFS? Justify your answer.
- (b) (2 points) What part would change in the code for DFS? What would be the runtime for DFS? Justify your answer.

## 6. DAG (1 point)

Is the graph above a directed acyclic graph (DAG)? Justify your answer.