## 3343 Analysis of Algorithms – Fall 11

## Schedule

8/7/11

(subject to change)

| Date      | Material   |                           |  |
|-----------|--|---------------------------|--|
| Th 8/25   | Analyzing algorithms (Ch. 2.2)   |                           |  |
|           | Best case and worst case runtimes; insertion sort, increment   | al algorithm              |  |
|           |  | No recitation             |  |
| Tu 8/30   | Asymptotic notation (Ch. 3, Ch. A)   |                           |  |
|           | $O, \Omega, \Theta, o, \text{ limit-theorem}; \text{ runtime for code-snippets}$   |                           |  |
|           | Homework 1 assigned  | Recitation: Homework 1    |  |
| Th $9/1$  | Asymptotic notation (Ch. 3, Ch. A)   |                           |  |
|           | $O, \Omega, \Theta, o, \text{ limit-theorem; runtime for code-snippets}$   | Recitation: Homework 1    |  |
| Tu 9/6    | Heapsort (Ch. 6)   |                           |  |
|           | Abstract data types (ADT), priority queue, heap, heapsort,   | <del>-</del>              |  |
|           | Homework 1 due; homework 2 assigned  | Recitation: Homework 2    |  |
| Th 9/8    | Recursion trees and induction (+)  |                           |  |
|           | Recursive algorithms. Guess solution of recurrence using rec   | <del>-</del>              |  |
|           | the correctness of the solution using induction.   | Recitation: Homework 2    |  |
| Tu 9/13   | Divide-and-conquer (Ch. 2.3) and recurrences (Ch. 4.3, 4.4)  |                           |  |
|           | Divide-and-conquer, merge sort, binary search; Runtime recu  | irrences. Big-Oh induc-   |  |
|           | tion (substitution method)   | D '' '' II l o            |  |
| TDI 0 /15 | Homework 2 due; homework 3 assigned  | Recitation: Homework 3    |  |
| Th 9/15   | Master theorem (Ch. 4.5)   | D '44' II 10              |  |
| TD 0/00   | Use of master theorem to solve recurrences.  | Recitation: Homework 3    |  |
| Tu 9/20   | More divide-and-conquer (Ch. 31.6 pages 956–957; 4.2)  |                           |  |
|           | Repeated squaring for exponentiation, Strassen's matrix mu   | _                         |  |
| Th. 0 /22 | Homework 3 due; homework 4 assigned; project 1 assigned Recitation: Homework 4  Probability, random variables and expected values (Ch. C.2, C.3) |                           |  |
| Th 9/22   | Probability, random variables, expected values.  | Recitation: Homework 4    |  |
| Tu 9/27   | Randomized algorithms (Ch. 5.1–5.3)  | itecitation. Homework 4   |  |
| 10 3/21   | Hiring problem; Expected runtime analysis.   |                           |  |
|           | Homework 4 due; homework 5 assigned  | Recitation: Homework 5    |  |
| Th 9/29   | Quicksort (Ch. 7.1–7.4)  | receitation. Homework 9   |  |
| 111 5/25  | Quicksort, best-case and worst-case runtimes, randomized q   | uicksort                  |  |
|           | Quichost, sess case and worst case randings, randomized q  | Recitation: Homework 5    |  |
| Tu 10/4   | Sorting (Ch. 8.1, 8.2, 8.3)  |                           |  |
|           | Decision trees, lower $\Omega(n \log n)$ bound for comparison sorts, $\alpha$  | counting sort, radix sort |  |
|           | Homework 5 due; homework 6 assigned; project 1 due   | Recitation: Review Test 1 |  |
| Th 10/6   | Order statistics (Ch. 9)   |                           |  |
| /         | Order statistics (find <i>i</i> -th smallest element); Randomized se   | election, deterministic   |  |
|           | selection in linear time.  | Recitation: Review Test 1 |  |
| Tu 10/11  | Test 1   |                           |  |
| - 32 - 37 | Material until 9/27 (inclusive)  | Recitation: Homework 6    |  |
| Th 10/13  | Red-black trees (Ch. 13.1, 13.2, 13.3)   |                           |  |
| 111 10/10 | Red-black tree property, rotations, insertion; abstract data   | types. ADT dictionary     |  |
|           | 2000 Property, Totalians, Informati, application data  | Recitation: Homework 6    |  |
| Tu 10/18  | B-trees (Ch. 18.1, 18.2)   |                           |  |
|           | k-ary search trees, B-tree def., height, insertion   |                           |  |
|           | Homework 6 due; homework 7 assigned; project 2 assigned  | Recitation: Homework 7    |  |
|           | ======== project & designed  |                           |  |

| Date  | Material  |  |  |
|---|---|--|--|
| Th 10/20                                    | Dynamic programming (Ch. 15.4, +)   |  |  |
| ,   | Fibonacci, binomial coefficient, LCS: fill table, then const  | truct solution from the  |  |
|   | table.  | Recitation: Homework 7   |  |
| Tu 10/25                                    | Dynamic programming (Ch. 15.3, 15.4., 16.2, +)  |  |  |
|   | 0-1 Knapsack; general outline of dynamic programming:   | Optimal substructure (re-  |  |
|   | currence), overlapping subproblems, fill table bottom-up  | or by memoization.   |  |
|   | Homework 7 due; homework 8 assigned   | Recitation: Homework 8   |  |
| Th $10/27$                                  | Greedy algorithms (Ch. 16.2, problem 16-1 on page 402)  |  |  |
|   | Greedy algorithms (greedy-choice property, optimal subst  | , – – .  |  |
|   | fractional knapsack.  | Recitation: Homework 8   |  |
| Tu 11/1                                     | Elementary Graph Algorithms (Ch. 22.1–22.2)   |  |  |
|   | Representations of graphs, breadth-first search (BFS)   |  |  |
|   | Homework 8 due; homework 9 assigned; project 2 due  | Recitation: Homework 9   |  |
| Th $11/3$                                   | Elementary Graph Algorithms (Ch. 22.3–22.4)   |  |  |
|   | Depth-first search (DFS), topological sort  | Recitation: Homework 9   |  |
| Tu 11/8                                     | Minimum Spanning Trees (Ch. 23)   | (0. 7.7  |  |
|   | Prim (grows single tree), Kruskal (grows forest; uses unio  | • •  |  |
|   | Homework 9 due; homework 10 assigned  | Recitation: Review Test 2  |  |
| Th $11/10$                                  | Single-source shortest paths (Ch. 24 without 24.4)  |  |  |
|   | Optimal substructure, triangle inequality, relaxation step  |  |  |
|   | negative edge weights), predecessor tree (shortest path tr  | ee); Bellman-Ford, detec-  |  |
|   | tion of negative-weight cycles; Shortest paths in a DAG.  |  |  |
|   | 1 D . 10 . 1  | $\mathbf{D} \cdot \mathbf{M} \cdot $ |  |
| - 11 /12                                    | Project 3 assigned  | Recitation: Review Test 2  |  |
| Tu 11/15                                    | Test 2  | Recitation: Review Test 2  |  |
| Tu 11/15                                    |   |  |  |
| ·   | Test 2 Material from 9/23 until 10/26 (inclusive)   | Recitation: Review Test 2  Recitation: Homework 10   |  |
| Tu 11/15 Th 11/17                           | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2)  | Recitation: Homework 10  |  |
| Th 11/17                                    | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  |  |  |
| ·   | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall P and NP (Ch. 34)  | Recitation: Homework 10  Recitation: Homework 10   |  |
| Th 11/17                                    | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP-  |  |
| Th 11/17                                    | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-completeness.  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP-  |  |
| Th 11/17                                    | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP-complete by reducing from   |  |
| Th 11/17 Tu 11/22                           | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned   | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP-  |  |
| Th 11/17                                    | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving   | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP-complete by reducing from   |  |
| Th 11/17 Tu 11/22 Th 11/24                  | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving No class  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP-complete by reducing from   |  |
| Th 11/17 Tu 11/22                           | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34)  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation   |  |
| Th 11/17 Tu 11/22 Th 11/24                  | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation  ath, Hamilton Circuit  |  |
| Th 11/17 Tu 11/22 Th 11/24 Tu 11/29         | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P Recitation: Homew  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation   |  |
| Th 11/17 Tu 11/22 Th 11/24                  | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P Recitation: Homework Approximation Algorithms (Ch. 35.1 and 35.2)   | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation  ath, Hamilton Circuit  oork 11, Review Final Exam  |  |
| Th 11/17 Tu 11/22 Th 11/24 Tu 11/29         | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-conter problems Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P Recitation: Homew Approximation Algorithms (Ch. 35.1 and 35.2) Constant factor approximation; Vertex cover; MST for En  | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation  ath, Hamilton Circuit rork 11, Review Final Exam  uclidean TSP.  |  |
| Th 11/17 Tu 11/22 Th 11/24 Tu 11/29 Th 12/1 | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P  Recitation: Homew  Approximation Algorithms (Ch. 35.1 and 35.2) Constant factor approximation; Vertex cover; MST for Execitation: Homew                         | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation  ath, Hamilton Circuit  oork 11, Review Final Exam  |  |
| Th 11/17 Tu 11/22 Th 11/24 Tu 11/29         | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P  Recitation: Homew  Approximation Algorithms (Ch. 35.1 and 35.2) Constant factor approximation; Vertex cover; MST for Exercitation: Homew  Review for Final Exam | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation  ath, Hamilton Circuit rork 11, Review Final Exam  uclidean TSP.  |  |
| Th 11/17 Tu 11/22 Th 11/24 Tu 11/29 Th 12/1 | Test 2 Material from 9/23 until 10/26 (inclusive)  All-Pairs Shortest Paths (Ch. 25.2) Dynamic programming: Floyd-Warshall  P and NP (Ch. 34) Decision problems, definition of classes P and NP, polyno hardness, NP-completeness; Show that problems are NP-cother problems  Homework 10 due; homework 11 assigned  Thanksgiving No class  P and NP (Ch. 34) TSP, Clique, Independent Set, Vertex Cover, Hamilton P  Recitation: Homew  Approximation Algorithms (Ch. 35.1 and 35.2) Constant factor approximation; Vertex cover; MST for Execitation: Homew                         | Recitation: Homework 10  Recitation: Homework 10  mial-time reductions, NP- complete by reducing from  No recitation  ath, Hamilton Circuit rork 11, Review Final Exam  uclidean TSP.  |  |

Chapter numbers refer to the CLRS book, 3rd edition.

The comprehensive final exam will be on Thursday 12/15, 10:30am – 1pm.

<sup>&</sup>quot;+" indicates additional material.