## CS 2233 Discrete Mathematical Structures - Fall 08

## Material relevant for the Final Exam

- Homeworks 1-8


## - 1.1-1.4 Logic:

- Propositions and operators (and, or, not, implication, etc.), truth tables
- Predicates and quantifiers (for-all, exists), nested quantifiers
- Translating a formula (with or without quantifiers) into English, and translating an English sentence into a formula
- Equivalences of formulas (e.g., De Morgan's Laws)
- NOT: Rules of inference (1.5)


## - 1.6-1.7 Proofs

- Different types of proofs (see handout; e.g., direct proof, proof by contradiction, proof by cases)
- Know how to apply different proof techniques to prove a theorem. (This includes, as a first step, translating an English statement into a propositional formula.)
- Know how to disprove a theorem (e.g., find a counterexample to disprove a for-all statement)
- 2.1-2.4 Sets, Functions, Sequences, Summations
- Sets: Definition, operators (intersection, union,...), power set, cartesian product
- Functions: Definition of a function, one-to-one/injective, onto/surjective, one-to-one correspondence/bijection, inverse, composition, graphs
- Sequences: Definition (functions with domain $\mathbb{N}$ )
- Summations: Know how to read the $\sum$ symbol, arithmetic series, geometric series, index substitution


## - 3.1-3.3 Algorithms and Complexity:

$-\mathrm{O}, \Omega, \Theta$. (E.g., use definitions to show that $4 n+5 \in O\left(n^{2}\right)$.)

- Code snippets


## - 4.1-4.2 Induction

- Weak and strong induction
- NOT: Program correctness and loop invariants (4.5)


## - 4.3, 7.1 Recursive Definitions and Recurrence Relations

- Recursive functions, sequences, and algorithms

Know how to develop a recursive solution (i.e., function, sequence, or algorithm) for a problem. (E.g., recursive function for $2^{n}$, or a recursive definition for the sequence $1,5,9,13,17, \ldots$ )

- Every recursive definition has a base case and a recursive case.
- Understand all recursive examples (Fibonacci, $n!$, Towers of Hanoi)
- Other recursive definitions (sets, arithmetic formulae)
- Recursive algorithms, and solving divide-and-conquer runtime recurrences (Handout from CLRS book, and parts of 7.3)
- Divide and conquer examples: Mergesort, recursive squaring
- NOT: Develop a divide and conquer algorithm
- Extract runtime recurrence from a recursive algorithm
- Solve the runtime recurrence:
* Generate a guess using either the expansion method or the recursion tree method (knowing any one method is enough)
* Big-Oh induction
* Master Theorem (The theorem itself will be given on the test, so you don't need to memorize it.)
- NOT: Solving linear recurrence relations (7.2)
- 8.1, 8.2, 8.5 Relations
- Definition of binary relations and of $k$-ary relations, binary relation on a set
- Properties of relations (reflexive, symmetric, antisymmetric, transitive)
- Equivalence relations, mod, equivalence classes
- NOT: Combining relations (union, intersection), databases and relations
- 9.1-9.3, 10.1 Graphs and Trees
- Definition of graph (undirected, directed), terminology (vertices, edges, degree, adjacent, incident, ...)
- Handshaking theorem (for undirected and for directed graphs)
- Representation of graphs: Adjacency matrix, adjacency lists.
- NOT: Special types of graphs (bipartite, complete,...), new graphs from old, graph isomorphisms, incidence matrix
- Definition of trees as acyclic connected undirected graphs, cycles, connectivity
- Rooted trees and notation (e.g., parent, children, height, descendants, internal vertex, leaf), $k$-ary trees, full trees
- Proofs (e.g., induction) on trees and graphs
- 12.1 Languages and Grammars
- Definitions of languages and grammars (vocabulary, terminal symbols, productions, etc.)
- Productions and derivability
- Backus Naur Form
- NOT: Derivation trees, types of grammars
- NOT: Finite State Machines (12.3)

The Final is on Friday December 12 from 7:30am until 10am in the classroom. It is closed-book and closed-notes, but you are allowed to bring one cheat sheet (a whole one-sided letter page). The Final will contain an exact copy of one question from the first midterm and the second midterm each.

