CS 2233 Discrete Mathematical Structures – Fall 08 Material relevant for the Final Exam

• Homeworks 1–8

• 1.1–1.4 Logic:

- Propositions and operators (and, or, not, implication, etc.), truth tables
- Predicates and quantifiers (for-all, exists), nested quantifiers
- Translating a formula (with or without quantifiers) into English, and translating an English sentence into a formula
- Equivalences of formulas (e.g., De Morgan's Laws)
- **NOT:** Rules of inference (1.5)

• 1.6–1.7 Proofs

- Different types of proofs (see handout; e.g., direct proof, proof by contradiction, proof by cases)
- Know how to apply different proof techniques to prove a theorem. (This includes, as a first step, translating an English statement into a propositional formula.)
- Know how to disprove a theorem (e.g., find a counterexample to disprove a for-all statement)

• 2.1–2.4 Sets, Functions, Sequences, Summations

- Sets: Definition, operators (intersection, union,...), power set, cartesian product
- Functions: Definition of a function, one-to-one/injective, onto/surjective, one-to-one correspondence/bijection, inverse, composition, graphs
- Sequences: Definition (functions with domain \mathbb{N})
- Summations: Know how to read the \sum symbol, arithmetic series, geometric series, index substitution

• 3.1-3.3 Algorithms and Complexity:

- O, Ω , Θ . (E.g., use definitions to show that $4n + 5 \in O(n^2)$.)
- Code snippets
- 4.1-4.2 Induction
 - Weak and strong induction
 - **NOT:** Program correctness and loop invariants (4.5)

• 4.3, 7.1 Recursive Definitions and Recurrence Relations

- Recursive functions, sequences, and algorithms
 Know how to develop a recursive solution (i.e., function, sequence, or algorithm) for a problem. (E.g., recursive function for 2ⁿ, or a recursive definition for the sequence 1, 5, 9, 13, 17,)
- Every recursive definition has a base case and a recursive case.

- Understand all recursive examples (Fibonacci, n!, Towers of Hanoi)
- Other recursive definitions (sets, arithmetic formulae)
- Recursive algorithms, and solving divide-and-conquer runtime recurrences (Handout from CLRS book, and parts of 7.3)
 - Divide and conquer examples: Mergesort, recursive squaring
 - **NOT:** Develop a divide and conquer algorithm
 - Extract runtime recurrence from a recursive algorithm
 - Solve the runtime recurrence:
 - * Generate a guess using either the expansion method or the recursion tree method (knowing any one method is enough)
 - * Big-Oh induction
 - * Master Theorem (The theorem itself will be given on the test, so you don't need to memorize it.)
- **NOT:** Solving linear recurrence relations (7.2)

• 8.1, 8.2, 8.5 Relations

- Definition of binary relations and of k-ary relations, binary relation on a set
- Properties of relations (reflexive, symmetric, antisymmetric, transitive)
- Equivalence relations, mod, equivalence classes
- NOT: Combining relations (union, intersection), databases and relations

• 9.1–9.3, 10.1 Graphs and Trees

- Definition of graph (undirected, directed), terminology (vertices, edges, degree, adjacent, incident, ...)
- Handshaking theorem (for undirected and for directed graphs)
- Representation of graphs: Adjacency matrix, adjacency lists.
- NOT: Special types of graphs (bipartite, complete,...), new graphs from old, graph isomorphisms, incidence matrix
- Definition of trees as acyclic connected undirected graphs, cycles, connectivity
- Rooted trees and notation (e.g., parent, children, height, descendants, internal vertex, leaf), k-ary trees, full trees
- Proofs (e.g., induction) on trees and graphs

• 12.1 Languages and Grammars

- Definitions of languages and grammars (vocabulary, terminal symbols, productions, etc.)
- Productions and derivability
- Backus Naur Form
- **NOT:** Derivation trees, types of grammars
- **NOT:** Finite State Machines (12.3)

The Final is on Friday December 12 from 7:30am until 10am in the classroom. It is closed-book and closed-notes, but you are allowed to bring one cheat sheet (a whole one-sided letter page). The Final will contain an exact copy of one question from the first midterm and the second midterm each.