### CMPS 2200 Introduction to Algorithms – Fall 12

10/24/12

# Programming Project 2 Due 12/4/12, 11:55pm on Blackboard

## Single Source Shortest Paths (45 points)

The goal of this project is to practice Java, Java's drawing functionality, graph manipulation, and some graph algorithms. You will implement Bellman-Ford's and Dijkstra's single source shortest paths algorithms, as well as Prim's MST algorithm, using a graph stored in adjacency lists. You can use any data structure to store the lists, as long as the overall storage is only  $\Theta(|E|)$ .

#### Files

- project2-dijkstra.zip contains java code for the project, including a Vertex class, basic drawing functionality, and an implementation of a heap. Please download this project and add your code to it. If you are using Eclipse you can import the project by importing this archive file directly.
- The project directory contains four data files storing example graphs: graph.dat is a directed graph with positive edge weights, graphUndirected.dat is an undirected graph with positive edge weights, graphNeg.dat is a directed graph with negative edge weights but without negative-weight cycles, and graphNegCycle.dat is a directed graph that contains a negative-weight cycle. The format of these files is as follows:
  - All numbers in the files are integers separated by spaces or line breaks. The first line contains the number n of vertices. Vertices in the file are identified with integers  $0 \dots n 1$ .
  - The following lines contain descriptions of the adjacency lists. Each list is described as follows:
    - \* The first line contains the ID, the x-coordinate, and the y-coordinate of the vertex v "owning" the adjacency list.
    - \* The second line contains the length l of the list (so,  $l = \deg(v)$ ).
    - \* The next l lines each contain a vertex ID and an integer weight (for the edge from v to the vertex in this line).

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#### Tasks

- 1. (10 points) Implement code that reads a directed weighted graph from a file into an adjacency list structure, and that draws the graph on the screen using the provided routines. Assume the file is given in the format described above.
- 2. (10 points) Implement Bellman-Ford's algorithm. In the absence of negative-weight cycles, the output should minimally include a) the source vertex, b) the shortest path tree, and c) the resulting d-values, and should be drawn overlayed on the graph on screen. If the graph contains a negative-weight cycle, the algorithm should detect this and output a corresponding message.
- 3. (10 points) Implement Dijkstra's algorithm. The output should minimally include a) the source vertex, b) the shortest path tree, and c) the resulting d-values, and should be drawn overlayed on the graph on screen.
- 4. (5 points) Implement Prim's algorithm. The output should minimally include a) the source vertex used to run Prim, b) the minimum spanning tree, and c) the resulting d-values (keys), and should be drawn overlayed on the graph on screen.
- 5. (10 points) Test your algorithms using an appropriate set of input graphs, and write a short report. You may want to add screen shots to the report. For your tests, use at least the graph data files provided with the project. Run Dijkstra, Bellman-Ford, and possibly Prim on the same inputs and compare the outputs. What happens in the case of negative weights or negative weight cycles?

#### **Turnin instructions**

- For this project, you have to use Java and you have to extend the provided project file.
- Do not use any other fancy libraries.
- Please include comments on how you compiled the project, and how to run tests.
- The name of your project directory should be project2\_<lastName><firstName>
- Zip up a directory with your entire project (source code and report). Turn in the zip file on Blackboard.
- All projects need to compile and run. If your program does not compile and run you will receive 0 points on this project.